

Multi-objective Optimization Framework for Energy Efficiency and Production Scheduling in Smart Manufacturing Using Reinforcement Learning and Digital Twin Technology Integration

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